

# Package: POPInf (via r-universe)

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**Type** Package

**Title** Assumption-Learn and Data-Adaptive Post-Prediction Inference

**Version** 1.0.0

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**Description** Implementation of assumption-learn and data-adaptive post-prediction inference (POPInf), for valid and efficient statistical inference based on data predicted by machine learning. See Miao, Miao, Wu, Zhao, and Lu (2023) <arXiv:2311.14220>.

**URL** <https://arxiv.org/abs/2311.14220>,  
<https://github.com/qlu-lab/POPInf>

**Depends** R (>= 3.5.0),

**Imports** randomForest, MASS

**License** GPL-3

**Encoding** UTF-8

**RoxygenNote** 7.2.3

**Repository** <https://qlu-lab.r-universe.dev>

**RemoteUrl** <https://github.com/qlu-lab/popinf>

**RemoteRef** HEAD

**RemoteSha** 6177791fef82ecf7c55ec9d89aba3419547e99f

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A	<i>Calculation of the matrix A based on single dataset</i>
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### Description

A function for the calculation of the matrix A based on single dataset

### Usage

A(X, Y, quant = NA, theta, method)

### Arguments

X	Array or DataFrame containing covariates
Y	Array or DataFrame of outcomes
quant	quantile for quantile estimation
theta	parameter theta
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

### Value

matrix A based on single dataset

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est_ini	<i>Initial estimation</i>
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### Description

est\_ini function for initial estimation

### Usage

est\_ini(X, Y, quant = NA, method)

**Arguments**

X	Array or DataFrame containing covariates
Y	Array or DataFrame of outcomes
quant	quantile for quantile estimation
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

initial estimator

---

link_grad	<i>gradient of the link function</i>
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**Description**

link\_grad function for gradient of the link function

**Usage**

```
link_grad(t, method)
```

**Arguments**

t	t
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

gradient of the link function

---

link_Hessian	<i>Hessians of the link function</i>
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---

**Description**

link\_Hessian function for Hessians of the link function

**Usage**

```
link_Hessian(t, method)
```

**Arguments**

t	t
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

Hessians of the link function

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mean_psi	<i>Sample expectation of psi</i>
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**Description**

mean\_psi function for sample expectation of psi

**Usage**

```
mean_psi(X, Y, theta, quant = NA, method)
```

**Arguments**

X	Array or DataFrame containing covariates
Y	Array or DataFrame of outcomes
theta	parameter theta
quant	quantile for quantile estimation
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

sample expectation of psi

---

`mean_psi_pop`*Sample expectation of POP-Inf psi*

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**Description**

`mean_psi_pop` function for sample expectation of POP-Inf psi

**Usage**

```
mean_psi_pop(  
  X_lab,  
  X_unlab,  
  Y_lab,  
  Yhat_lab,  
  Yhat_unlab,  
  w,  
  theta,  
  quant = NA,  
  method  
)
```

**Arguments**

<code>X_lab</code>	Array or DataFrame containing observed covariates in labeled data.
<code>X_unlab</code>	Array or DataFrame containing observed or predicted covariates in unlabeled data.
<code>Y_lab</code>	Array or DataFrame of observed outcomes in labeled data.
<code>Yhat_lab</code>	Array or DataFrame of predicted outcomes in labeled data.
<code>Yhat_unlab</code>	Array or DataFrame of predicted outcomes in unlabeled data.
<code>w</code>	weights vector POP-Inf linear regression (d-dimensional, where d equals the number of covariates).
<code>theta</code>	parameter theta
<code>quant</code>	quantile for quantile estimation
<code>method</code>	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

sample expectation of POP-Inf psi

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 optim\_est

*Gradient descent for obtaining estimator*


---

### Description

optim\_est function for gradient descent for obtaining estimator

### Usage

```
optim_est(
  X_lab,
  X_unlab,
  Y_lab,
  Yhat_lab,
  Yhat_unlab,
  w,
  theta,
  quant = NA,
  method,
  step_size = 0.1,
  max_iterations = 500,
  convergence_threshold = 1e-06
)
```

### Arguments

X_lab	Array or DataFrame containing observed covariates in labeled data.
X_unlab	Array or DataFrame containing observed or predicted covariates in unlabeled data.
Y_lab	Array or DataFrame of observed outcomes in labeled data.
Yhat_lab	Array or DataFrame of predicted outcomes in labeled data.
Yhat_unlab	Array or DataFrame of predicted outcomes in unlabeled data.
w	weights vector POP-Inf linear regression (d-dimensional, where d equals the number of covariates).
theta	parameter theta
quant	quantile for quantile estimation
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".
step_size	step size for gradient descent
max_iterations	maximum of iterations for gradient descent
convergence_threshold	convergence threshold for gradient descent

### Value

estimator

---

`optim_weights`*Gradient descent for obtaining the weight vector*

---

**Description**

`optim_weights` function for gradient descent for obtaining estimator

**Usage**

```
optim_weights(  
  j,  
  X_lab,  
  X_unlab,  
  Y_lab,  
  Yhat_lab,  
  Yhat_unlab,  
  w,  
  theta,  
  quant = NA,  
  method  
)
```

**Arguments**

<code>j</code>	<code>j</code> -th coordinate of weights vector
<code>X_lab</code>	Array or DataFrame containing observed covariates in labeled data.
<code>X_unlab</code>	Array or DataFrame containing observed or predicted covariates in unlabeled data.
<code>Y_lab</code>	Array or DataFrame of observed outcomes in labeled data.
<code>Yhat_lab</code>	Array or DataFrame of predicted outcomes in labeled data.
<code>Yhat_unlab</code>	Array or DataFrame of predicted outcomes in unlabeled data.
<code>w</code>	weights vector POP-Inf linear regression ( $d$ -dimensional, where $d$ equals the number of covariates).
<code>theta</code>	parameter $\theta$
<code>quant</code>	quantile for quantile estimation
<code>method</code>	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

weights

pop\_M

*POP-Inf M-Estimation***Description**

pop\_M function conducts post-prediction M-Estimation.

**Usage**

```
pop_M(
  X_lab = NA,
  X_unlab = NA,
  Y_lab,
  Yhat_lab,
  Yhat_unlab,
  alpha = 0.05,
  weights = NA,
  max_iterations = 100,
  convergence_threshold = 0.05,
  quant = NA,
  intercept = FALSE,
  focal_index = NA,
  method
)
```

**Arguments**

X_lab	Array or DataFrame containing observed covariates in labeled data.
X_unlab	Array or DataFrame containing observed or predicted covariates in unlabeled data.
Y_lab	Array or DataFrame of observed outcomes in labeled data.
Yhat_lab	Array or DataFrame of predicted outcomes in labeled data.
Yhat_unlab	Array or DataFrame of predicted outcomes in unlabeled data.
alpha	Specifies the confidence level as 1 - alpha for confidence intervals.
weights	weights vector POP-Inf linear regression (d-dimensional, where d equals the number of covariates).
max_iterations	Sets the maximum number of iterations for the optimization process to derive weights.
convergence_threshold	Sets the convergence threshold for the optimization process to derive weights.
quant	quantile for quantile estimation
intercept	Boolean indicating if the input covariates' data contains the intercept (TRUE if the input data contains)
focal_index	Identifies the focal index for variance reduction.
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".



**Value**

A summary table presenting point estimates, standard error, confidence intervals (1 - alpha), P-values, and weights.

**Examples**

```
data <- sim_data()
X_lab <- data$X_lab
X_unlab <- data$X_unlab
Y_lab <- data$Y_lab
Yhat_lab <- data$Yhat_lab
Yhat_unlab <- data$Yhat_unlab
pop_M(Y_lab = Y_lab, Yhat_lab = Yhat_lab, Yhat_unlab = Yhat_unlab,
      alpha = 0.05, method = "mean")
pop_M(Y_lab = Y_lab, Yhat_lab = Yhat_lab, Yhat_unlab = Yhat_unlab,
      alpha = 0.05, quant = 0.75, method = "quantile")
pop_M(X_lab = X_lab, X_unlab = X_unlab,
      Y_lab = Y_lab, Yhat_lab = Yhat_lab, Yhat_unlab = Yhat_unlab,
      alpha = 0.05, method = "ols")
```

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 psi

*Esimating equation*


---

**Description**

psi function for esimating equation

**Usage**

```
psi(X, Y, theta, quant = NA, method)
```

**Arguments**

X	Array or DataFrame containing covariates
Y	Array or DataFrame of outcomes
theta	parameter theta
quant	quantile for quantile estimation
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

esimating equation

---

Sigma_cal	<i>Variance-covariance matrix of the estimation equation</i>
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---

**Description**

Sigma\_cal function for variance-covariance matrix of the estimation equation

**Usage**

```
Sigma_cal(
  X_lab,
  X_unlab,
  Y_lab,
  Yhat_lab,
  Yhat_unlab,
  w,
  theta,
  quant = NA,
  A_lab_inv,
  A_unlab_inv,
  method
)
```

**Arguments**

X_lab	Array or DataFrame containing observed covariates in labeled data.
X_unlab	Array or DataFrame containing observed or predicted covariates in unlabeled data.
Y_lab	Array or DataFrame of observed outcomes in labeled data.
Yhat_lab	Array or DataFrame of predicted outcomes in labeled data.
Yhat_unlab	Array or DataFrame of predicted outcomes in unlabeled data.
w	weights vector POP-Inf linear regression (d-dimensional, where d equals the number of covariates).
theta	parameter theta
quant	quantile for quantile estimation
A_lab_inv	Inverse of matrix A using labeled data
A_unlab_inv	Inverse of matrix A using unlabeled data
method	indicates the method to be used for M-estimation. Options include "mean", "quantile", "ols", "logistic", and "poisson".

**Value**

variance-covariance matrix of the estimation equation

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sim_data	<i>Simulate the data for testing the functions</i>
----------	--

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**Description**

sim\_data function for the calculation of the matrix A

**Usage**

```
sim_data(r = 0.9, binary = FALSE)
```

**Arguments**

r	imputation correlation
binary	simulate binary outcome or not

**Value**

simulated data

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